



Work: Example Model

Author:

Model: **SteelFrame.axs**

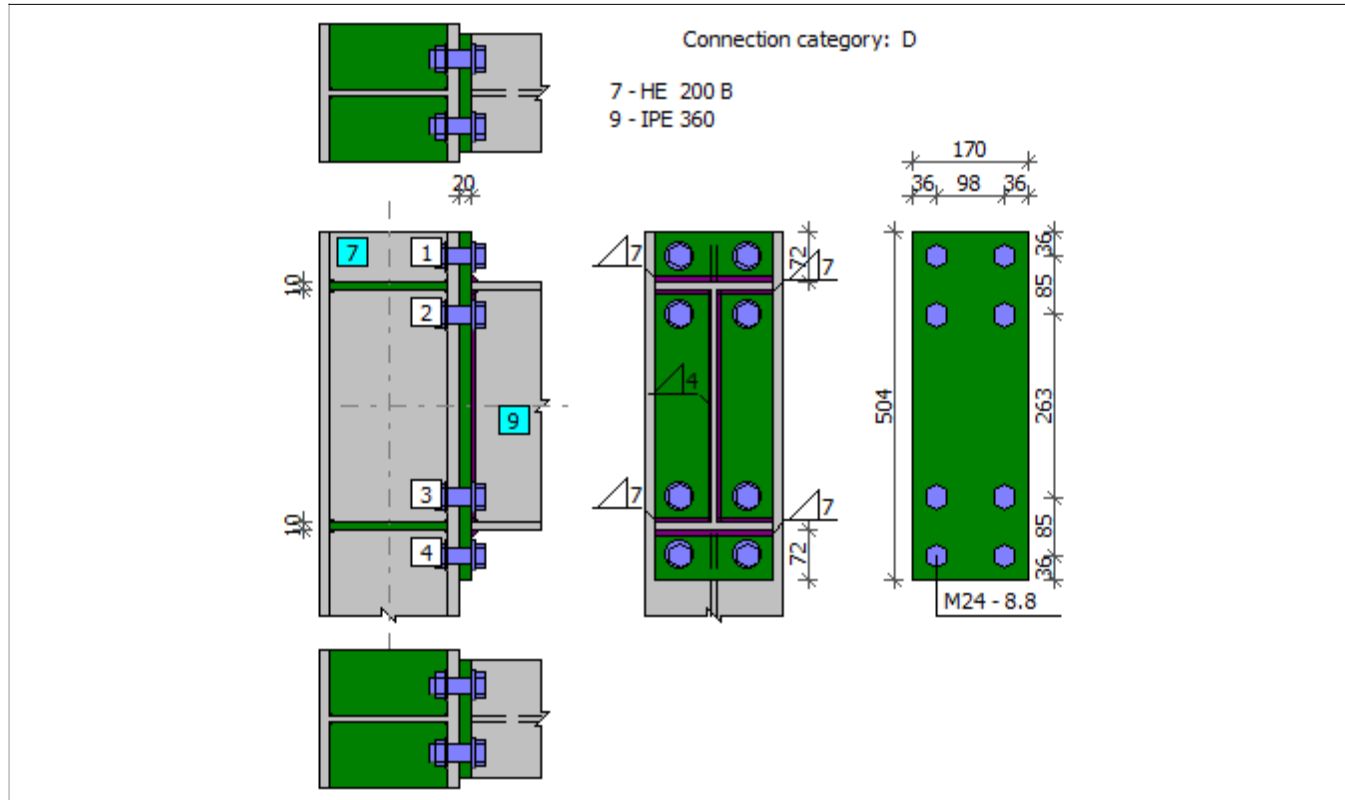
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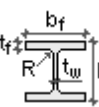
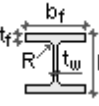
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	Beam - column (front plate) EC3 1991-1-8: 2008	Ratio : 0.81	
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Structure node: 14

Structure bars: 7, 9

**Data**

Column HE 200 B					
	h_c	b_{fc}	t_{fc}	t_{wc}	R_c
	200.00mm	200.00mm	15.00mm	9.00mm	0.00mm
	A_c	J_{y0c}	J_{z0c}	y_{0c}	z_{0c}
	78.08cm ²	5696.17cm ⁴	2003.37cm ⁴	100.00mm	100.00mm
Material	Grade	f_y	f_u		
	S 355	355.00MPa	510.00MPa		
Beam IPE 360					
	h_b	b_{fb}	t_{fb}	t_{wb}	R_b
	360.00mm	170.00mm	12.70mm	8.00mm	0.00mm
	A_b	J_{y0b}	J_{z0b}	y_{0b}	z_{0b}
	72.73cm ²	16270.00cm ⁴	1043.45cm ⁴	85.00mm	180.00mm
Material	Grade	f_y	f_u		
	S 355	355.00MPa	510.00MPa		

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Front plate			
	l_p	h_p	t_p
	170.00mm	504.00mm	20.00mm
Material	Grade	f_y	f_u
	S 355	355.00MPa	510.00MPa

Bolts connecting front plate and column flange

Grade		8.8
Yield point	$f_y =$	640.00MPa
Resistance on tension	$f_u =$	800.00MPa
Bolt diameter	$d =$	24.00mm
Bolt opening diameter	$d_0 =$	27.00mm
Area of bolt section	$A =$	4.52cm ²
Effective section area of a bolt	$A_s =$	3.53cm ²
Number of rows	$w =$	4.00mm
Distance from horizontal edge	$e_1 =$	36.00mm
Horizontal spacing	$w_1 =$	98.00mm
Number of bolts in rows		$m_1 = 2; m_2 = 2; m_3 = 2; m_4 = 2$
Vertical spacing of rows		$p_1 = 84.70mm; p_2 = 262.60mm; p_3 = 84.70mm$

Welds

Thickness of fillet welds connecting beam flanges and front plate	$a_f =$	7.00mm
Thickness of fillet welds connecting beam web and front plate	$a_w =$	4.00mm

Materials coeffs

Coefficient	$\gamma_{M0} =$	1.00
Coefficient	$\gamma_{M1} =$	1.00
Coefficient	$\gamma_{M2} =$	1.25

Forces**Design loads Co #2**

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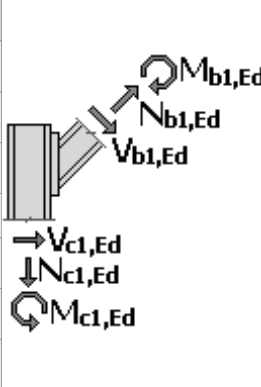
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Right beam		
Axial force	$N_{b1,Ed} =$	$-44.28kN$
Shear force	$V_{b1,Ed} =$	$62.88kN$
Bending moment	$M_{b1,Ed} =$	$113.42kNm$
Lower column		
Axial force	$N_{c1,Ed} =$	$-85.29kN$
Shear force	$V_{c1,Ed} =$	$44.44kN$
Bending moment	$M_{c1,Ed} =$	$113.34kNm$


Results

Column web panel in shear

The section area of column web panel

$$A_{vc} = A_c - 2 \cdot b_{fc} \cdot t_{fc} + (t_{wc} + 2 \cdot r_c) \cdot t_{fc} = 78.08cm^2 - 2 \cdot 200.00mm \cdot 15.00mm + (9.00mm + 2 \cdot 0.00mm) \cdot 15.00mm = 19.43cm^2$$

The plastic moment resistance of a column flange

$$M_{pl,fc,Rd} = \frac{0.25 \cdot b_{fc} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 200.00mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 3.99kNm$$

The distance between the centrelines of the stiffeners

$$d_s = 347.30mm$$

The plastic moment resistance of a stiffener-top flange level of beam

$$M_{pl,stu,Rd} = \frac{0.25 \cdot b_{fc} \cdot t_{sfu}^2 \cdot f_{ys}}{\gamma_{M0}} = \frac{0.25 \cdot 200.00mm \cdot (10.00mm)^2 \cdot 355.00MPa}{1.00} = 0.17kNm$$

The plastic moment resistance of a stiffener-bottom flange level of beam

$$M_{pl,ssl,Rd} = \frac{0.25 \cdot b_{fc} \cdot t_{sfl}^2 \cdot f_{ys}}{\gamma_{M0}} = \frac{0.25 \cdot 200.00mm \cdot (10.00mm)^2 \cdot 355.00MPa}{1.00} = 0.17kNm$$

The additional shear resistance due to stiffeners

$$V_{wp,add,Rd} = \min\left(\frac{4 \cdot M_{pl,fc,Rd}}{d_s}; \frac{2 \cdot M_{pl,fc,Rd} + 2 \cdot M_{pl,st,Rd}}{d_s}\right) = \min\left(\frac{4 \cdot 3.99kNm}{347.30mm}; \frac{2 \cdot 3.99kNm + 2 \cdot 0.34kNm}{347.30mm}\right) = 24.95kN$$

The plastic shear resistance of a column web panel

$$V_{wp,Rd} = \frac{0.9 \cdot A_{vc} \cdot f_{ywc}}{\sqrt{3} \cdot \gamma_{M0}} + V_{wp,add,Rd} = \frac{0.9 \cdot 19.43cm^2 \cdot 355.00MPa}{\sqrt{3} \cdot 1.00} + 24.95kN = 383.36kN$$

The resulting shear force in the web panel

$$V_{wp,Ed} = \frac{M_{b1,Ed} - M_{b2,Ed}}{z} - 0.5 \cdot (V_{c1,Ed} - V_{c2,Ed}) = \frac{113.42kNm - 0.00kNm}{347.30mm} - 0.5 \cdot (44.44kN - 0.00kN) = 304.35kN$$

$ V_{wp,Ed} \leq V_{wp,Rd}$	$ 304.35kN < 383.36kN$	0.79	✓
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Column web in transverse compression

Calculation parameter

$$s_p = \min(t_p + c; 2 \cdot t_p) = \min(20.00mm + 72.00mm; 2 \cdot 20.00mm) = 40.00mm$$

The effective width of the column web in compression

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$$b_{eff,c,wc} = t_{fb} + 2 \cdot \sqrt{2} \cdot a_f + 5 \cdot (t_{fc} + r_c) + s_p = 12.70mm + 2 \cdot \sqrt{2} \cdot 7.00mm + 5 \cdot (15.00mm + 0.00mm) + 40.00mm = 147.50mm$$

Reduction factor

$$\omega_1 = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{b_{eff,c,wc} \cdot t_{wc}}{A_{vc}} \right)^2}} = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{147.50 \cdot 9.00mm}{19.43cm^2} \right)^2}} = 0.79$$

$$\omega = \omega_1 = 0.79$$

Design resistance of column web subject to transverse compression

$$F_{c,wc,Rd1} = \frac{\omega \cdot k_{wc} \cdot b_{eff,c,wc} \cdot t_{wc} \cdot f_{y,wc}}{\gamma_{M0}} = \frac{0.79 \cdot 1.00 \cdot 147.50mm \cdot 9.00mm \cdot 355.00MPa}{1.00} = 371.77kN$$

The depth of the column web

$$d_{wc} = h_c - 2 \cdot (t_{fc} + r_c) = 200.00mm - 2 \cdot (15.00mm + 0.00mm) = 170.00mm$$

Plate slenderness

$$\lambda_p = 0.932 \cdot \sqrt{\frac{b_{eff,c,wc} \cdot d_{wc} \cdot f_{y,wc}}{E \cdot t_{wc}^2}} = 0.932 \cdot \sqrt{\frac{147.50mm \cdot 170.00mm \cdot 355.00MPa}{210000.00MPa \cdot (9.00mm)^2}} = 0.67$$

The reduction factor for plate buckling

$$\rho = \frac{\lambda_p - 0.22}{\lambda_p^2} = \frac{0.67 - 0.22}{(0.67)^2} = 1.00$$

$$F_{c,wc,Rd2} = \frac{\omega \cdot k_{wc} \cdot \rho \cdot b_{eff,c,wc} \cdot t_{wc} \cdot f_{y,wc}}{\gamma_{M1}} = \frac{0.79 \cdot 1.00 \cdot 1.00 \cdot 147.50mm \cdot 9.00mm \cdot 355.00MPa}{1.00} = 371.77kN$$

$$F_{c,wc,Rd,st} = \frac{(b_{fc} - t_{wc}) \cdot t_s \cdot f_{y,s}}{\gamma_{M0}} = \frac{(200.00mm - 9.00mm) \cdot 10.00mm \cdot 355.00MPa}{1.00} = 678.05kN$$

Design resistance of column web subject to transverse compression

$$F_{c,wc,Rd} = \min(F_{c,wc,Rd1}; F_{c,wc,Rd2}) + F_{c,wc,Rd,st} = \min(371.77kN; 371.77kN) + 678.05kN = 1049.82kN$$

Beam flange and web in compression

Plastic section modulus

$$W_{pl} = 973.74cm^3$$

The design resistance for bending of cross-section

$$M_{c,Rd} = \frac{W_{pl} \cdot f_{yb}}{\gamma_{M0}} = \frac{973.74cm^3 \cdot 355.00MPa}{1.00} = 345.68kNm$$

Distance between beam flanges

$$h_f = 347.30mm$$

Design resistance of flange beam subject compression

$$F_{c,fb,Rd} = \frac{M_{c,Rd}}{h_f} = \frac{345.68kNm}{347.30mm} = 995.32kN$$

Bolts connecting front plate and column flange

Tensile resistance of a bolt

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$$F_{t,Rd} = \frac{k_2 \cdot f_{ub} \cdot A_s}{\gamma_{M2}} = \frac{0.90 \cdot 800.00 \text{MPa} \cdot 3.53 \text{cm}^2}{1.25} = 203.33 \text{kN}$$

Shear section area of bolt

$$A = 0.25 \cdot \pi \cdot d^2 = 0.25 \cdot \pi \cdot (24.00 \text{mm})^2 = 4.52 \text{cm}^2$$

Shear resistance of bolt in one surface

$$F_{v,Rd} = \frac{\alpha_v \cdot m \cdot f_{ub} \cdot A}{\gamma_{M2}} = \frac{0.60 \cdot 1 \cdot 800.00 \text{MPa} \cdot 4.52 \text{cm}^2}{1.25} = 173.72 \text{kN}$$

Punching shear resistance of a bolt

$$B_{p,Rd} = \frac{0.6 \cdot \pi \cdot d_m \cdot t_{fc} \cdot f_{uc}}{\gamma_{M2}} = \frac{0.6 \cdot \pi \cdot 37.99 \text{mm} \cdot 15.00 \text{mm} \cdot 510.00 \text{MPa}}{1.25} = 438.25 \text{kN}$$

Tension zone

BOLTS ROW 1

Column flange in bending

Geometrical parameters

Bolt distance from upper edge column

$$e_{1fc} = e_c + e_1 = 0.00 \text{mm} + 36.00 \text{mm} = 36.00 \text{mm}$$

Bolt distance from outer edge

$$e_{fc} = 51.00 \text{mm}$$

Bolt distance from column web

$$m_{fc} = 0.5 \cdot (w - t_{wc}) - 0.8 \cdot r_c = 0.5 \cdot (98.00 \text{mm} - 9.00 \text{mm}) - 0.8 \cdot 0.00 \text{mm} = 44.50 \text{mm}$$

Distance $e\{\min\}$

$$e_{\min} = 36.00 \text{mm}$$

Calculation parameter n

$$n = \min(e_{\min}; 1.25 \cdot m_{fc}) = \min(36.00 \text{mm}; 1.25 \cdot 44.50 \text{mm}) = 51.00 \text{mm}$$

Calculation parameter

$$m_{2fc} = p_1 + e_1 - e_{p1} - t_{fb} - 0.8 \cdot a_f \cdot \sqrt{2} = 84.70 \text{mm} + 36.00 \text{mm} - 72.00 \text{mm} - 15.00 \text{mm} - 0.8 \cdot 7.00 \text{mm} \cdot \sqrt{2} = 383.99 \text{mm}$$

$$\lambda_1 = \frac{m_{fc}}{m_{fc} + e_{fc}} = \frac{44.50 \text{mm}}{44.50 \text{mm} + 51.00 \text{mm}} = 0.47$$

$$\lambda_2 = \frac{m_{2fc}}{m_{fc} + e_{fc}} = \frac{383.99 \text{mm}}{44.50 \text{mm} + 51.00 \text{mm}} = 4.02$$

$$\alpha = 5.44$$

Effective length for one bolt in circular patterns

$$l_{\text{eff,cp},1} = 2 \cdot \pi \cdot m_{fc} = 2 \cdot \pi \cdot 44.50 \text{mm} = 279.60 \text{mm}$$

$$l_{\text{eff,cp},2} = \pi \cdot m_{fc} + 2 \cdot e_1 = \pi \cdot 44.50 \text{mm} + 2 \cdot 51.00 \text{mm} = 211.80 \text{mm}$$

$$l_{\text{eff,cp}} = \min(l_{\text{eff,cp},1}; l_{\text{eff,cp},2}) = \min(279.60 \text{mm}; 211.80 \text{mm}) = 211.80 \text{mm}$$

Effective length for one bolt in non-circular patterns

$$l_{\text{eff,nc}} = e_1 + \alpha \cdot m_{fc} - (2 \cdot m_{fc} + 0.625 \cdot e) = 36.00 \text{mm} + 5.44 \cdot 44.50 \text{mm} - (2 \cdot 44.50 \text{mm} + 0.625 \cdot 51.00 \text{mm}) = 157.21 \text{mm}$$

Effective length for one bolt for 1 mode

$$l_{\text{eff},1} = \min(l_{\text{eff,cp}}; l_{\text{eff,nc}}) = \min(211.80 \text{mm}; 157.21 \text{mm}) = 157.21 \text{mm}$$

Effective length for one bolt for 2 mode

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$$l_{eff,2} = l_{eff,nc} = 157.21mm$$

Model 1: Complete yielding of the column flange

$$M_{pl,1,Rd} = \frac{0.25 \cdot l_{eff,1} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 157.21mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 3.14kNm$$

Method 1

$$F_{T,1,Rd1} = \frac{4 \cdot M_{pl,1,Rd}}{m_{fc}} = \frac{4 \cdot 3.14kNm}{44.50mm} = 282.18kN$$

Method 2 (alternative method)

Parameter for bearing zone

$$e_w = 0.25 \cdot d_w = 0.25 \cdot 44.00mm = 11.00mm$$

$$F_{T,1,Rd2} = \frac{(8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}}{2 \cdot m_{fc} \cdot n - e_w \cdot (m_{fc} + n)} = \frac{(8 \cdot 51.00mm - 2 \cdot 11.00mm) \cdot 3.14kNm}{2 \cdot 44.50mm \cdot 51.00mm - 11.00mm \cdot (44.50mm + 51.00mm)} = 347.35kN$$

$$F_{T,1,Rd} = \min(F_{T,1,Rd1}; F_{T,1,Rd2}) = \min(282.18kN; 347.35kN) = 282.18kN$$

Model 2: Bolt failure with yielding of the column flange

$$M_{pl,2,Rd} = \frac{0.25 \cdot l_{eff,2} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 157.21mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 3.14kNm$$

$$F_{T,2,Rd} = \frac{2 \cdot M_{pl,2,Rd} + n \cdot \sum F_{t,Rd}}{m_{fc} + n} = \frac{2 \cdot 3.14kNm + 51.00mm \cdot 2 \cdot 203.33kN}{44.50mm + 51.00mm} = 282.91kN$$

Model 3: Bolt failure

$$F_{T,3,Rd} = \sum F_{t,Rd} = 2 \cdot 203.33kN = 406.66kN$$

Component resistance

$$F_{t,fc,Rd(1)} = \min(F_{T,1,Rd}; F_{T,2,Rd}; F_{T,3,Rd}) = \min(282.18kN; 282.91kN; 406.66kN) = 282.18kN$$

Column web in transverse tension

The section area of column web panel

$$A_{vc} = A_c - 2 \cdot b_{fc} \cdot t_{fc} + (t_{wc} + r_c) \cdot t_{fc} = 78.08cm^2 - 2 \cdot 200.00mm \cdot 15.00mm + (9.00mm + 0.00mm) \cdot 15.00mm = 19.43cm^2$$

The effective width of the column web in tension

$$b_{eff,t,wc} = l_{eff,1(1)} = 157.21mm$$

Reduction factor

$$\omega_1 = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{b_{eff,t,wc} \cdot t_{wc}}{A_{vc}} \right)^2}} = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{157.21 \cdot 9.00mm}{19.43cm^2} \right)^2}} = 0.77$$

$$\omega = \omega_1 = 0.77$$

$$F_{t,wc,Rd,st} = \frac{(b_{fc} - t_{wc}) \cdot t_s \cdot f_{y,s}}{\gamma_{M0}} = \frac{(200.00mm - 9.00mm) \cdot 10.00mm \cdot 355.00MPa}{1.00} = 678.05kN$$

Design resistance of column web subject to transverse tension

$$F_{t,wc,Rd(1)} = \frac{\omega \cdot b_{eff,t,wc} \cdot t_{wc} \cdot f_{y,wc}}{\gamma_{M0}} + F_{t,wc,Rd,st} = \frac{0.77 \cdot 157.21mm \cdot 9.00mm \cdot 355.00MPa}{1.00} + 678.05kN = 1064.49kN$$

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End plate in bending

Geometrical parameters

Bolt distance from outer edge

$$e_{ep} = 36.00mm$$

Bolt distance from beam web

$$m_{ep} = 0.5 \cdot (w - t_{wb}) - 0.8 \cdot \sqrt{2} \cdot a_w = 0.5 \cdot (98.00mm - 8.00mm) - 0.8 \cdot \sqrt{2} \cdot 4.00mm = 40.47mm$$

Distance e_{\min}

$$e_{\min} = \min(e_x; e_{ep}) = \min(36.00mm; 36.00mm) = 36.00mm$$

Calculation parameter n

$$n = \min(e_{\min}; 1.25 \cdot m_{ep}) = \min(36.00mm; 1.25 \cdot 40.47mm) = 35.10mm$$

Bolt distance from beam flange

$$m_x = e_{p1} - e_1 - 0.8 \cdot a_f \cdot \sqrt{2} = 72.00mm - 36.00mm - 0.8 \cdot 7.00mm \cdot \sqrt{2} = 28.08mm$$

Bolt distance from outer horizontal edge plate

$$e_x = e_1 = 36.00mm$$

Effective length for one bolt in circular patterns

$$l_{eff,cp,1} = 2 \cdot \pi \cdot m_x = 2 \cdot \pi \cdot 28.08mm = 176.43mm$$

$$l_{eff,cp,2} = \pi \cdot m_x + w = \pi \cdot 28.08mm + 98.00mm = 186.22mm$$

$$l_{eff,cp,3} = \pi \cdot m_x + 2 \cdot e = \pi \cdot 28.08mm + 2 \cdot 36.00mm = 160.22mm$$

$$l_{eff,cp} = \min(l_{eff,cp,1}; l_{eff,cp,2}; l_{eff,cp,3}) = \min(176.43mm; 186.22mm; 160.22mm) = 160.22mm$$

Effective length for one bolt in non-circular patterns

$$l_{eff,nc,1} = 4 \cdot m_x + 1.25 \cdot e_x = 4 \cdot 28.08mm + 1.25 \cdot 36.00mm = 157.32mm$$

$$l_{eff,nc,2} = e + 2 \cdot m_x + 0.625 \cdot e_x = 36.00mm + 2 \cdot 28.08mm + 0.625 \cdot 36.00mm = 114.66mm$$

$$l_{eff,nc,3} = 0.5 \cdot b_p = 0.5 \cdot 170.00mm = 85.00mm$$

$$l_{eff,nc,4} = 0.5 \cdot w + 2 \cdot m_x + 0.625 \cdot e_x = 0.5 \cdot 98.00mm + 2 \cdot 28.08mm + 0.625 \cdot 36.00mm = 127.66mm$$

$$l_{eff,nc} = \min(l_{eff,nc,1}; l_{eff,nc,2}; l_{eff,nc,3}; l_{eff,nc,4}) = \min(157.32mm; 114.66mm; 85.00mm; 127.66mm) = 85.00mm$$

Effective length for one bolt for 1 mode

$$l_{eff,1} = \min(l_{eff,cp}; l_{eff,nc}) = \min(160.22mm; 85.00mm) = 85.00mm$$

Effective length for one bolt for 2 mode

$$l_{eff,2} = l_{eff,nc} = 85.00mm$$

Model 1: Complete yielding of the end plate

$$M_{pl,1,Rd} = \frac{0.25 \cdot l_{eff,1} \cdot t_p^2 \cdot f_{yp}}{\gamma_{M0}} = \frac{0.25 \cdot 85.00mm \cdot (20.00mm)^2 \cdot 355.00MPa}{1.00} = 3.02kNm$$

Method 1

$$F_{T,1,Rd1} = \frac{4 \cdot M_{pl,1,Rd}}{m_x} = \frac{4 \cdot 3.02kNm}{28.08mm} = 429.84kN$$

Method 2 (alternative method)

Parameter for bearing zone

$$e_w = 0.25 \cdot d_w = 0.25 \cdot 44.00mm = 11.00mm$$

$$F_{T,1,Rd2} = \frac{(8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}}{2 \cdot m_x \cdot n - e_w \cdot (m_x + n)} = \frac{(8 \cdot 35.10mm - 2 \cdot 11.00mm) \cdot 3.02kNm}{2 \cdot 28.08mm \cdot 35.10mm - 11.00mm \cdot (28.08mm + 35.10mm)} = 611.89kN$$

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$$F_{T,1,Rd} = \min(F_{T,1,Rd1}; F_{T,1,Rd2}) = \min(429.84kN; 611.89kN) = 429.84 \text{ kN}$$

Model 2: Bolt failure with yielding of the end plate

$$M_{pl,2,Rd} = \frac{0.25 \cdot l_{eff,2} \cdot t_p^2 \cdot f_{yp}}{\gamma_{M0}} = \frac{0.25 \cdot 85.00mm \cdot (20.00mm)^2 \cdot 355.00MPa}{1.00} = 3.02kNm$$

$$F_{T,2,Rd} = \frac{2 \cdot M_{pl,2,Rd} + n \cdot \sum F_{t,Rd}}{m_x + n} = \frac{2 \cdot 3.02kNm + 35.10mm \cdot 2 \cdot 203.33kN}{28.08mm + 35.10mm} = 321.44kN$$

Model 3: Bolt failure

$$F_{T,3,Rd} = \sum F_{t,Rd} = 2 \cdot 203.33kN = 406.66kN$$

Component resistance

$$F_{t,ep,Rd(1)} = \min(F_{T,1,Rd}; F_{T,2,Rd}; F_{T,3,Rd}) = \min(429.84kN; 321.44kN; 406.66kN) = 321.44 \text{ kN}$$

Resistance of the bolt row 1

$F_{t,Rd(1)M} = \min$	
· $F_{t,fc,Rd(1)} =$	282.18kN
· $F_{t,wc,Rd(1)} =$	1064.49kN
· $F_{t,ep,Rd(1)} =$	321.44kN
· $\frac{V_{wp,Rd}}{\beta} =$	$\frac{383.36kN}{1.00} = 383.36kN$
· $F_{cwc,Rd} =$	1049.82kN
· $F_{cfb,Rd} =$	995.32kN
= 282.18kN	

BOLTS ROW 2

Column flange in bending

Geometrical parameters

Bolt distance from outer edge

$$e_{fc} = 51.00mm$$

Bolt distance from column web

$$m_{fc} = 0.5 \cdot (w - t_{wc}) - 0.8 \cdot r_c = 0.5 \cdot (98.00mm - 9.00mm) - 0.8 \cdot 0.00mm = 44.50mm$$

Distance e{min}

$$e_{min} = 36.00mm$$

Calculation parameter n

$$n = \min(e_{min}; 1.25 \cdot m_{fc}) = \min(36.00mm; 1.25 \cdot 44.50mm) = 51.00mm$$

Effective length for one bolt in circular patterns

$$l_{eff,cp} = 2 \cdot \pi \cdot m_{fc} = 2 \cdot \pi \cdot 44.50mm = 279.60mm$$

Effective length for one bolt in non-circular patterns

$$l_{eff,nc} = 4 \cdot m_{fc} + 1.25 \cdot e = 4 \cdot 44.50mm + 1.25 \cdot 51.00mm = 241.75mm$$

Effective length for one bolt for 1 mode

$$l_{eff,1} = \min(l_{eff,cp}; l_{eff,nc}) = \min(279.60mm; 241.75mm) = 241.75mm$$

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Effective length for one bolt for 2 mode

$$l_{eff,2} = l_{eff,nc} = 241.75mm$$

Model 1: Complete yielding of the column flange

$$M_{pl,1,Rd} = \frac{0.25 \cdot l_{eff,1} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 241.75mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 4.83kNm$$

Method 1

$$F_{T,1,Rd1} = \frac{4 \cdot M_{pl,1,Rd}}{m_{fc}} = \frac{4 \cdot 4.83kNm}{44.50mm} = 433.93kN$$

Method 2 (alternative method)

Parameter for bearing zone

$$e_w = 0.25 \cdot d_w = 0.25 \cdot 44.00mm = 11.00mm$$

$$F_{T,1,Rd2} = \frac{(8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}}{2 \cdot m_{fc} \cdot n - e_w \cdot (m_{fc} + n)} = \frac{(8 \cdot 51.00mm - 2 \cdot 11.00mm) \cdot 4.83kNm}{2 \cdot 44.50mm \cdot 51.00mm - 11.00mm \cdot (44.50mm + 51.00mm)} = 534.15kN$$

$$F_{T,1,Rd} = \min(F_{T,1,Rd1}; F_{T,1,Rd2}) = \min(433.93kN; 534.15kN) = 433.93kN$$

Model 2: Bolt failure with yielding of the column flange

$$M_{pl,2,Rd} = \frac{0.25 \cdot l_{eff,2} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 241.75mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 4.83kNm$$

$$F_{T,2,Rd} = \frac{2 \cdot M_{pl,2,Rd} + n \cdot \sum F_{t,Rd}}{m_{fc} + n} = \frac{2 \cdot 4.83kNm + 51.00mm \cdot 2 \cdot 203.33kN}{44.50mm + 51.00mm} = 318.27kN$$

Model 3: Bolt failure

$$F_{T,3,Rd} = \sum F_{t,Rd} = 2 \cdot 203.33kN = 406.66kN$$

Component resistance

$$F_{t,fc,Rd(1)} = \min(F_{T,1,Rd}; F_{T,2,Rd}; F_{T,3,Rd}) = \min(433.93kN; 318.27kN; 406.66kN) = 318.27kN$$

Column web in transverse tension

The section area of column web panel

$$A_{vc} = A_c - 2 \cdot b_{fc} \cdot t_{fc} + (t_{wc} + r_c) \cdot t_{fc} = 78.08cm^2 - 2 \cdot 200.00mm \cdot 15.00mm + (9.00mm + 0.00mm) \cdot 15.00mm = 19.43cm^2$$

The effective width of the column web in tension

$$b_{eff,t,wc} = l_{eff,1(2)} = 241.75mm$$

Reduction factor

$$\omega_1 = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{b_{eff,t,wc} \cdot t_{wc}}{A_{vc}} \right)^2}} = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{241.75 \cdot 9.00mm}{19.43cm^2} \right)^2}} = 0.62$$

$$\omega = \omega_1 = 0.62$$

$$F_{t,wc,Rd,st} = \frac{(b_{fc} - t_{wc}) \cdot t_s \cdot f_{y,s}}{\gamma_{M0}} = \frac{(200.00mm - 9.00mm) \cdot 10.00mm \cdot 355.00MPa}{1.00} = 678.05kN$$

Design resistance of column web subject to transverse tension

$$F_{t,wc,Rd(2)} = \frac{\omega \cdot b_{eff,t,wc} \cdot t_{wc} \cdot f_{y,wc}}{\gamma_{M0}} + F_{t,wc,Rd,st} = \frac{0.62 \cdot 241.75mm \cdot 9.00mm \cdot 355.00MPa}{1.00} + 678.05kN = 1154.32kN$$

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End plate in bending

Geometrical parameters

Bolt distance from outer edge

$$e_{ep} = 36.00mm$$

Bolt distance from beam web

$$m_{ep} = 0.5 \cdot (w - t_{wb}) - 0.8 \cdot \sqrt{2} \cdot a_w = 0.5 \cdot (98.00mm - 8.00mm) - 0.8 \cdot \sqrt{2} \cdot 4.00mm = 40.47mm$$

Distance $e\{\min\}$

$$e_{min} = 36.00mm$$

Calculation parameter n

$$n = \min(e_{min}; 1.25 \cdot m_{ep}) = \min(36.00mm; 1.25 \cdot 40.47mm) = 36.00mm$$

Calculation parameter

$$m_{2ep} = p_1 + e_1 - e_{p1} - t_{fb} - 0.8 \cdot a_f \cdot \sqrt{2} = 84.70mm + 36.00mm - 72.00mm - 12.70mm - 0.8 \cdot 7.00mm \cdot \sqrt{2} = 28.08mm$$

$$\lambda_1 = \frac{m_{ep}}{m_{ep} + e_{ep}} = \frac{40.47mm}{40.47mm + 36.00mm} = 0.53$$

$$\lambda_2 = \frac{m_{2ep}}{m_{ep} + e_{ep}} = \frac{28.08mm}{40.47mm + 36.00mm} = 0.37$$

$$\alpha = 5.88$$

Effective length for one bolt in circular patterns

$$l_{eff,cp} = 2 \cdot \pi \cdot m_{ep} = 2 \cdot \pi \cdot 40.47mm = 254.31mm$$

Effective length for one bolt in non-circular patterns

$$l_{eff,nc} = \alpha \cdot m_{ep} = 5.88 \cdot 40.47mm = 238.05mm$$

Effective length for one bolt for 1 mode

$$l_{eff,1} = \min(l_{eff,cp}; l_{eff,nc}) = \min(254.31mm; 238.05mm) = 238.05mm$$

Effective length for one bolt for 2 mode

$$l_{eff,2} = l_{eff,nc} = 238.05mm$$

Model 1: Complete yielding of the end plate

$$M_{pl,1,Rd} = \frac{0.25 \cdot l_{eff,1} \cdot t_p^2 \cdot f_{yp}}{\gamma_{M0}} = \frac{0.25 \cdot 238.05mm \cdot (20.00mm)^2 \cdot 355.00MPa}{1.00} = 8.45kNm$$

Method 1

$$F_{T,1,Rd1} = \frac{4 \cdot M_{pl,1,Rd}}{m_{ep}} = \frac{4 \cdot 8.45kNm}{40.47mm} = 835.18kN$$

Method 2 (alternative method)

Parameter for bearing zone

$$e_w = 0.25 \cdot d_w = 0.25 \cdot 44.00mm = 11.00mm$$

$$F_{T,1,Rd2} = \frac{(8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}}{2 \cdot m_{ep} \cdot n - e_w \cdot (m_{ep} + n)} = \frac{(8 \cdot 36.00mm - 2 \cdot 11.00mm) \cdot 8.45kNm}{2 \cdot 40.47mm \cdot 36.00mm - 11.00mm \cdot (40.47mm + 36.00mm)} = 1084.42kN$$

$$F_{T,1,Rd} = \min(F_{T,1,Rd1}; F_{T,1,Rd2}) = \min(835.18kN; 1084.42kN) = 835.18kN$$

Model 2: Bolt failure with yielding of the end plate

$$M_{pl,2,Rd} = \frac{0.25 \cdot l_{eff,2} \cdot t_p^2 \cdot f_{yp}}{\gamma_{M0}} = \frac{0.25 \cdot 238.05mm \cdot (20.00mm)^2 \cdot 355.00MPa}{1.00} = 8.45kNm$$

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$$F_{T,2,Rd} = \frac{2 \cdot M_{pl,2,Rd} + n \cdot \sum F_{t,Rd}}{m_{ep} + n} = \frac{2 \cdot 8.45kNm + 36.00mm \cdot 2 \cdot 203.33kN}{40.47mm + 36.00mm} = 412.44kN$$

Model 3: Bolt failure

$$F_{T,3,Rd} = \sum F_{t,Rd} = 2 \cdot 203.33kN = 406.66kN$$

Component resistance

$$F_{t,ep,Rd(1)} = \min(F_{T,1,Rd}; F_{T,2,Rd}; F_{T,3,Rd}) = \min(835.18kN; 412.44kN; 406.66kN) = 406.66kN$$

Beam web in tension

Effective width of beam web in tension

$$b_{eff,t,wb} = l_{eff(2)} = 238.05mm$$

Component resistance

$$F_{t,wb,Rd(2)} = \frac{b_{eff,t,wb} \cdot t_{wb} \cdot f_{yb}}{\gamma_{M0}} = \frac{238.05mm \cdot 8.00mm \cdot 355.00MPa}{1.00} = 676.07kN$$

Resistance of the bolt row 2

$F_{t,Rd(2)M} = \min$			
·	$F_{t,fc,Rd(2)} =$	318.27kN	
·	$F_{t,wc,Rd(2)} =$	1154.32kN	
·	$F_{t,ep,Rd(2)} =$	406.66kN	
·	$F_{t,wb,Rd(2)} =$	676.07kN	
·	$\frac{V_{wp,Rd}}{\beta} - F_{t,Rd(1)M} =$	$\frac{383.36kN}{1.00} - 282.18kN =$	101.19kN
·	$F_{cwc,Rd} - F_{t,Rd(1)M} =$	$1049.82kN - 282.18kN =$	767.65kN
·	$F_{cfb,Rd} - F_{t,Rd(1)M} =$	$995.32kN - 282.18kN =$	713.15kN
			= 101.19kN

BOLTS ROW 3

Column flange in bending

Geometrical parameters

Bolt distance from outer edge

$$e_{fc} = 51.00mm$$

Bolt distance from column web

$$m_{fc} = 0.5 \cdot (w - t_{wc}) - 0.8 \cdot r_c = 0.5 \cdot (98.00mm - 9.00mm) - 0.8 \cdot 0.00mm = 44.50mm$$

Distance e{min}

$$e_{min} = 36.00mm$$

Calculation parameter n

$$n = \min(e_{min}; 1.25 \cdot m_{fc}) = \min(36.00mm; 1.25 \cdot 44.50mm) = 51.00mm$$

Effective length for one bolt in circular patterns

$$l_{eff,cp} = 2 \cdot \pi \cdot m_{fc} = 2 \cdot \pi \cdot 44.50mm = 279.60mm$$

Effective length for one bolt in non-circular patterns

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$$l_{eff,nc} = 4 \cdot m_{fc} + 1.25 \cdot e = 4 \cdot 44.50mm + 1.25 \cdot 51.00mm = 241.75mm$$

Effective length for one bolt for 1 mode

$$l_{eff,1} = \min(l_{eff,cp}; l_{eff,nc}) = \min(279.60mm; 241.75mm) = 241.75mm$$

Effective length for one bolt for 2 mode

$$l_{eff,2} = l_{eff,nc} = 241.75mm$$

Model 1: Complete yielding of the column flange

$$M_{pl,1,Rd} = \frac{0.25 \cdot l_{eff,1} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 241.75mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 4.83kNm$$

Method 1

$$F_{T,1,Rd1} = \frac{4 \cdot M_{pl,1,Rd}}{m_{fc}} = \frac{4 \cdot 4.83kNm}{44.50mm} = 433.93kN$$

Method 2 (alternative method)

Parameter for bearing zone

$$e_w = 0.25 \cdot d_w = 0.25 \cdot 44.00mm = 11.00mm$$

$$F_{T,1,Rd2} = \frac{(8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}}{2 \cdot m_{fc} \cdot n - e_w \cdot (m_{fc} + n)} = \frac{(8 \cdot 51.00mm - 2 \cdot 11.00mm) \cdot 4.83kNm}{2 \cdot 44.50mm \cdot 51.00mm - 11.00mm \cdot (44.50mm + 51.00mm)} = 534.15kN$$

$$F_{T,1,Rd} = \min(F_{T,1,Rd1}; F_{T,1,Rd2}) = \min(433.93kN; 534.15kN) = 433.93kN$$

Model 2: Bolt failure with yielding of the column flange

$$M_{pl,2,Rd} = \frac{0.25 \cdot l_{eff,2} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 241.75mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 4.83kNm$$

$$F_{T,2,Rd} = \frac{2 \cdot M_{pl,2,Rd} + n \cdot \sum F_{t,Rd}}{m_{fc} + n} = \frac{2 \cdot 4.83kNm + 51.00mm \cdot 2 \cdot 203.33kN}{44.50mm + 51.00mm} = 318.27kN$$

Model 3: Bolt failure

$$F_{T,3,Rd} = \sum F_{t,Rd} = 2 \cdot 203.33kN = 406.66kN$$

Component resistance

$$F_{t,fc,Rd(1)} = \min(F_{T,1,Rd}; F_{T,2,Rd}; F_{T,3,Rd}) = \min(433.93kN; 318.27kN; 406.66kN) = 318.27kN$$

Column web in transverse tension

The section area of column web panel

$$A_{vc} = A_c - 2 \cdot b_{fc} \cdot t_{fc} + (t_{wc} + r_c) \cdot t_{fc} = 78.08cm^2 - 2 \cdot 200.00mm \cdot 15.00mm + (9.00mm + 0.00mm) \cdot 15.00mm = 19.43cm^2$$

The effective width of the column web in tension

$$b_{eff,t,wc} = l_{eff,1(3)} = 241.75mm$$

Reduction factor

$$\omega_1 = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{b_{eff,t,wc} \cdot t_{wc}}{A_{vc}} \right)^2}} = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{241.75 \cdot 9.00mm}{19.43cm^2} \right)^2}} = 0.62$$

$$\omega = \omega_1 = 0.62$$

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$$F_{t,wc,Rd,st} = \frac{(b_{fc} - t_{wc}) \cdot t_s \cdot f_{y,s}}{\gamma_{M0}} = \frac{(200.00mm - 9.00mm) \cdot 10.00mm \cdot 355.00MPa}{1.00} = 678.05kN$$

Design resistance of column web subject to transverse tension

$$F_{t,wc,Rd(3)} = \frac{\omega \cdot b_{eff,t,wc} \cdot t_{wc} \cdot f_{y,wc}}{\gamma_{M0}} + F_{t,wc,Rd,st} = \frac{0.62 \cdot 241.75mm \cdot 9.00mm \cdot 355.00MPa}{1.00} + 678.05kN = 1154.32kN$$

End plate in bending

Geometrical parameters

Bolt distance from outer edge

$$e_{ep} = 36.00mm$$

Bolt distance from beam web

$$m_{ep} = 0.5 \cdot (w - t_{wb}) - 0.8 \cdot \sqrt{2} \cdot a_w = 0.5 \cdot (98.00mm - 8.00mm) - 0.8 \cdot \sqrt{2} \cdot 4.00mm = 40.47mm$$

Distance $e\{\min\}$

$$e_{min} = 36.00mm$$

Calculation parameter n

$$n = \min(e_{min}; 1.25 \cdot m_{ep}) = \min(36.00mm; 1.25 \cdot 40.47mm) = 36.00mm$$

Effective length for one bolt in circular patterns

$$l_{eff,cp} = 2 \cdot \pi \cdot m_{ep} = 2 \cdot \pi \cdot 40.47mm = 254.31mm$$

Effective length for one bolt in non-circular patterns

$$l_{eff,nc} = 4 \cdot m_{ep} + 1.25 \cdot e = 4 \cdot 40.47mm + 1.25 \cdot 36.00mm = 206.90mm$$

Effective length for one bolt for 1 mode

$$l_{eff,1} = \min(l_{eff,cp}; l_{eff,nc}) = \min(254.31mm; 206.90mm) = 206.90mm$$

Effective length for one bolt for 2 mode

$$l_{eff,2} = l_{eff,nc} = 206.90mm$$

Model 1: Complete yielding of the end plate

$$M_{pl,1,Rd} = \frac{0.25 \cdot l_{eff,1} \cdot t_p^2 \cdot f_{yp}}{\gamma_{M0}} = \frac{0.25 \cdot 206.90mm \cdot (20.00mm)^2 \cdot 355.00MPa}{1.00} = 7.34kNm$$

Method 1

$$F_{T,1,Rd1} = \frac{4 \cdot M_{pl,1,Rd}}{m_{ep}} = \frac{4 \cdot 7.34kNm}{40.47mm} = 725.88kN$$

Method 2 (alternative method)

Parameter for bearing zone

$$e_w = 0.25 \cdot d_w = 0.25 \cdot 44.00mm = 11.00mm$$

$$F_{T,1,Rd2} = \frac{(8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}}{2 \cdot m_{ep} \cdot n - e_w \cdot (m_{ep} + n)} = \frac{(8 \cdot 36.00mm - 2 \cdot 11.00mm) \cdot 7.34kNm}{2 \cdot 40.47mm \cdot 36.00mm - 11.00mm \cdot (40.47mm + 36.00mm)} = 942.49kN$$

$$F_{T,1,Rd} = \min(F_{T,1,Rd1}; F_{T,1,Rd2}) = \min(725.88kN; 942.49kN) = 725.88kN$$

Model 2: Bolt failure with yielding of the end plate

$$M_{pl,2,Rd} = \frac{0.25 \cdot l_{eff,2} \cdot t_p^2 \cdot f_{yp}}{\gamma_{M0}} = \frac{0.25 \cdot 206.90mm \cdot (20.00mm)^2 \cdot 355.00MPa}{1.00} = 7.34kNm$$

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$$F_{T,2,Rd} = \frac{2 \cdot M_{pl,2,Rd} + n \cdot \sum F_{t,Rd}}{m_{ep} + n} = \frac{2 \cdot 7.34kNm + 36.00mm \cdot 2 \cdot 203.33kN}{40.47mm + 36.00mm} = 383.52kN$$

Model 3: Bolt failure

$$F_{T,3,Rd} = \sum F_{t,Rd} = 2 \cdot 203.33kN = 406.66kN$$

Component resistance

$$F_{t,ep,Rd(1)} = \min(F_{T,1,Rd}; F_{T,2,Rd}; F_{T,3,Rd}) = \min(725.88kN; 383.52kN; 406.66kN) = 383.52kN$$

Beam web in tension

Effective width of beam web in tension

$$b_{eff,t,wb} = l_{eff(3)} = 206.90mm$$

Component resistance

$$F_{t,wb,Rd(3)} = \frac{b_{eff,t,wb} \cdot t_{wb} \cdot f_{yb}}{\gamma_{M0}} = \frac{206.90mm \cdot 8.00mm \cdot 355.00MPa}{1.00} = 587.59kN$$

Column flange in bending

Row 2+3 considered as group

Circular patterns**Bolts row 2**

$$l_{eff,cp(2,g)} = \pi \cdot m_{fc} + p = \pi \cdot 44.50mm + 262.60mm = 402.40mm$$

Bolts row 3

$$l_{eff,cp(3,g)} = \pi \cdot m_{fc} + p = \pi \cdot 44.50mm + 262.60mm = 402.40mm$$

$$\sum l_{eff(2+3)} = l_{eff,cp(2,g)} + l_{eff,cp(3,g)} = 402.40mm + 402.40mm = 804.80mm$$

Non-circular patterns**Bolts row 2**

$$l_{eff,nc(2,g)} = 2 \cdot m_{fc} + 0.625 \cdot e + 0.5 \cdot p = 2 \cdot 44.50mm + 0.625 \cdot 51.00mm + 0.5 \cdot 262.60mm = 252.18mm$$

Bolts row 3

$$l_{eff,nc(3,g)} = 2 \cdot m_{fc} + 0.625 \cdot e + 0.5 \cdot p = 2 \cdot 44.50mm + 0.625 \cdot 51.00mm + 0.5 \cdot 262.60mm = 252.18mm$$

$$\sum l_{eff,nc(2+3)} = l_{eff,nc(2,g)} + l_{eff,nc(3,g)} = 252.18mm + 252.18mm = 504.35mm$$

Model 1: Complete yielding of the column flange

Effective length for one bolt for 1 mode

$$\sum l_{eff,1(2+3)} = \min(\sum l_{eff,cp(2+3)}; \sum l_{eff,nc(2+3)}) = \min(804.80mm; 504.35mm) = 504.35mm$$

$$M_{pl,1,Rd} = \frac{0.25 \cdot \sum l_{eff,1(2+3)} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 504.35mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 10.07kNm$$

$$F_{T,1,Rd} = \frac{(8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}}{2 \cdot m \cdot n - e_w \cdot (m + n)} = \frac{(8 \cdot 51.00mm - 2 \cdot 11.00mm) \cdot 10.07kNm}{2 \cdot 44.50mm \cdot 51.00mm - 11.00mm \cdot (44.50mm + 51.00mm)} = 1114.38kN$$

Model 2: Bolt failure with yielding of the column flange

Effective length for one bolt for 2 mode

$$\sum l_{eff,2(2+3)} = \sum l_{eff,nc(2+3)} = 504.35mm$$

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$$M_{pl,2,Rd} = \frac{0.25 \cdot \sum l_{eff,2(2+3)} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 504.35mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 10.07kNm$$

$$F_{T,2,Rd} = \frac{2 \cdot M_{pl,2,Rd} + n \cdot \sum B_{p,Rd}}{m_{fc} + n} = \frac{2 \cdot 10.07kNm + 51.00mm \cdot 4 \cdot 203.33kN}{44.50mm + 51.00mm} = 645.25kN$$

Model 3: Bolt failure

$$F_{T,3,Rd} = \sum F_{t,Rd} = 4 \cdot 203.33kN = 813.31kN$$

Resistance of group

$$F_{t,fc(2+3)} = \min(F_{T,1,Rd}; F_{T,2,Rd}; F_{T,3,Rd}) = \min(905.28kN; 645.25kN; 813.31kN) = 645.25kN$$

Column web in transverse tension

The section area of column web panel

$$A_{vc} = A_c - 2 \cdot b_{fc} \cdot t_{fc} + (t_{wc} + r_c) \cdot t_{fc} = 78.08cm^2 - 2 \cdot 200.00mm \cdot 15.00mm + (9.00mm + 0.00mm) \cdot 15.00mm = 19.43cm^2$$

The effective width of the column web in tension

$$b_{eff,t,wc} = \sum l_{eff,1(2+3)} = 504.35mm$$

Reduction factor

$$\omega_1 = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{b_{eff,t,wc} \cdot t_{wc}}{A_{vc}} \right)^2}} = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{504.35 \cdot 9.00mm}{19.43cm^2} \right)^2}} = 0.35$$

$$\omega = \omega_1 = 0.35$$

$$F_{t,wc,Rd,st} = \frac{(b_{fc} - t_{wc}) \cdot t_s \cdot f_{y,s}}{\gamma_{M0}} = \frac{(200.00mm - 9.00mm) \cdot 10.00mm \cdot 355.00MPa}{1.00} = 678.05kN$$

Design resistance of column web subject to transverse tension

$$F_{t,wc,Rd(2+3)} = \frac{\omega \cdot b_{eff,t,wc} \cdot t_{wc} \cdot f_{y,wc}}{\gamma_{M0}} + F_{t,wc,Rd,st} = \frac{0.35 \cdot 504.35mm \cdot 9.00mm \cdot 355.00MPa}{1.00} + 678.05kN = 1244.42kN$$

End plate in bending

Row 2+3 considered as group

Circular patterns**Bolts row 2**

$$l_{eff,cp(2,g)} = \pi \cdot m_{ep} + p = \pi \cdot 40.47mm + 262.60mm = 389.75mm$$

Bolts row 3

$$l_{eff,cp(3,g)} = \pi \cdot m_{ep} + p = \pi \cdot 40.47mm + 262.60mm = 389.75mm$$

$$\sum l_{eff(2+3)} = l_{eff,cp(2,g)} + l_{eff,cp(3,g)} = 389.75mm + 389.75mm = 779.51mm$$

Non-circular patterns**Bolts row 2**

$$l_{eff,nc(2,g)} = 0.5 \cdot p + \alpha \cdot m_{ep} - (2 \cdot m_{ep} + 0.625 \cdot e) = 0.5 \cdot 262.60mm + 0.00 \cdot 40.47mm - (2 \cdot 40.47mm + 0.625 \cdot 36.00mm) = 265.91mm$$

Bolts row 3

$$l_{eff,nc(3,g)} = 2 \cdot m_{ep} + 0.625 \cdot e + 0.5 \cdot p = 2 \cdot 40.47mm + 0.625 \cdot 36.00mm + 0.5 \cdot 262.60mm = 234.75mm$$

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$$\sum l_{eff,nc(2+3)} = l_{eff,nc(2,g)} + l_{eff,nc(3,g)} = 265.91mm + 234.75mm = 500.65mm$$

Model 1: Complete yielding of the end plate

Effective length for one bolt for 1 mode

$$\sum l_{eff,1(2+3)} = \min(\sum l_{eff,cp(2+3)}; \sum l_{eff,nc(2+3)}) = \min(779.51mm; 500.65mm) = 500.65mm$$

$$M_{pl,1,Rd} = \frac{0.25 \cdot \sum l_{eff,1(2+3)} \cdot t_p^2 \cdot f_{yp}}{\gamma_{M0}} = \frac{0.25 \cdot 500.65mm \cdot (20.00mm)^2 \cdot 355.00MPa}{1.00} = 17.77kNm$$

Method 1

$$F_{T,1,Rd1} = \frac{4 \cdot M_{pl,1,Rd}}{m_{ep}} = \frac{4 \cdot 17.77kNm}{40.47mm} = 1756.49kN$$

Method 2 (alternative method)

$$F_{T,1,Rd2} = \frac{(8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}}{2 \cdot m_{ep} \cdot n - e_w \cdot (m_{ep} + n)} = \frac{(8 \cdot 36.00mm - 2 \cdot 11.00mm) \cdot 17.77kNm}{2 \cdot 40.47mm \cdot 36.00mm - 11.00mm \cdot (40.47mm + 36.00mm)} = 2280.66kN$$

$$F_{T,1,Rd} = \min(F_{T,1,Rd1}; F_{T,1,Rd2}) = \min(1756.49kN; 2280.66kN) = 1756.49kN$$

Model 2: Bolt failure with yielding of the end plate

Effective length for one bolt for 2 mode

$$\sum l_{eff,2(2+3)} = \sum l_{eff,nc(2+3)} = 500.65mm$$

$$M_{pl,2,Rd} = \frac{0.25 \cdot \sum l_{eff,2(2+3)} \cdot t_p^2 \cdot f_{yp}}{\gamma_{M0}} = \frac{0.25 \cdot 500.65mm \cdot (20.00mm)^2 \cdot 355.00MPa}{1.00} = 17.77kNm$$

$$F_{T,2,Rd} = \frac{2 \cdot M_{pl,2,Rd} + n \cdot \sum B_{p,Rd}}{m_{ep} + n} = \frac{2 \cdot 17.77kNm + 36.00mm \cdot 4 \cdot 203.33kN}{40.47mm + 36.00mm} = 847.68kN$$

Model 3: Bolt failure

$$F_{T,3,Rd} = \sum F_{t,Rd} = 4 \cdot 203.33kN = 813.31kN$$

Resistance of group

$$F_{t,ep(2+3)} = \min(F_{T,1,Rd}; F_{T,2,Rd}; F_{T,3,Rd}) = \min(1756.49kN; 847.68kN; 813.31kN) = 813.31kN$$

Beam web in tension

Effective width of beam web in tension

$$b_{eff,t,wb} = \sum l_{eff1(2+3)} = 500.65mm$$

Component resistance

$$F_{t,wb,Rd(2+3)} = \frac{b_{eff,t,wb} \cdot t_{wb} \cdot f_{yb}}{\gamma_{M0}} = \frac{500.65mm \cdot 8.00mm \cdot 355.00MPa}{1.00} = 1421.86kN$$

Resistance of the bolt row 3

$F_{t,Rd(3)M} = \min$	
· $F_{t,fc,Rd(3)} =$	318.27kN
· $F_{t,wc,Rd(3)} =$	1154.32kN

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· $F_{t,ep,Rd(3)} =$	383.52kN	
· $F_{t,wb,Rd(3)} =$	587.59kN	
· $F_{t,fc,Rd(2+3)} - F_{t,Rd(2)M} =$	645.25kN - 101.19kN =	544.06kN
· $F_{t,wc,Rd(2+3)} - F_{t,Rd(2)M} =$	1244.42kN - 101.19kN =	1143.23kN
· $F_{t,ep,Rd(2+3)} - F_{t,Rd(2)M} =$	813.31kN - 101.19kN =	712.12kN
· $F_{t,wb,Rd(2+3)} - F_{t,Rd(2)M} =$	1421.86kN - 101.19kN =	1320.67kN
· $\frac{V_{wp,Rd}}{\beta} - F_{t,Rd(1)M} - F_{t,Rd(2)M} =$	$\frac{383.36kN}{1.00} - 282.18kN - 101.19kN =$	0.00kN
· $F_{cwc,Rd} - F_{t,Rd(1)M} - F_{t,Rd(2)M} =$	1049.82kN - 282.18kN - 101.19kN =	666.46kN
· $F_{cfb,Rd} - F_{t,Rd(1)M} - F_{t,Rd(2)M} =$	995.32kN - 282.18kN - 101.19kN =	611.96kN
	= 0.00kN	

BOLTS ROW 4

Column flange in bending

Geometrical parameters

Bolt distance from upper edge column

$$e_{1fc} = e_c + e_1 = 0.00mm + 36.00mm = 36.00mm$$

Bolt distance from outer edge

$$e_{fc} = 51.00mm$$

Bolt distance from column web

$$m_{fc} = 0.5 \cdot (w - t_{wc}) - 0.8 \cdot r_c = 0.5 \cdot (98.00mm - 9.00mm) - 0.8 \cdot 0.00mm = 44.50mm$$

Distance e_{\min}

$$e_{\min} = 36.00mm$$

Calculation parameter n

$$n = \min(e_{\min}; 1.25 \cdot m_{fc}) = \min(36.00mm; 1.25 \cdot 44.50mm) = 51.00mm$$

Calculation parameter

$$m_{2fc} = p_1 + e_1 - e_{p1} - t_{fb} - 0.8 \cdot a_f \cdot \sqrt{2} = 84.70mm + 36.00mm - 72.00mm - 15.00mm - 0.8 \cdot 7.00mm \cdot \sqrt{2} = 48.01mm$$

$$\lambda_1 = \frac{m_{fc}}{m_{fc} + e_{fc}} = \frac{44.50mm}{44.50mm + 51.00mm} = 0.47$$

$$\lambda_2 = \frac{m_{2fc}}{m_{fc} + e_{fc}} = \frac{48.01mm}{44.50mm + 51.00mm} = 0.50$$

$$\alpha = 5.90$$

Effective length for one bolt in circular patterns

$$l_{eff,cp,1} = 2 \cdot \pi \cdot m_{fc} = 2 \cdot \pi \cdot 44.50mm = 279.60mm$$

$$l_{eff,cp,2} = \pi \cdot m_{fc} + 2 \cdot e_1 = \pi \cdot 44.50mm + 2 \cdot 51.00mm = 211.80mm$$

$$l_{eff,cp} = \min(l_{eff,cp,1}; l_{eff,cp,2}) = \min(279.60mm; 211.80mm) = 211.80mm$$

Effective length for one bolt in non-circular patterns

$$l_{eff,nc} = e_1 + \alpha \cdot m_{fc} - (2 \cdot m_{fc} + 0.625 \cdot e) = 36.00mm + 5.90 \cdot 44.50mm - (2 \cdot 44.50mm + 0.625 \cdot 51.00mm) = 177.59mm$$

Effective length for one bolt for 1 mode

$$l_{eff,1} = \min(l_{eff,cp}; l_{eff,nc}) = \min(211.80mm; 177.59mm) = 177.59mm$$

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Effective length for one bolt for 2 mode

$$l_{eff,2} = l_{eff,nc} = 177.59mm$$

Model 1: Complete yielding of the column flange

$$M_{pl,1,Rd} = \frac{0.25 \cdot l_{eff,1} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 177.59mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 3.55kNm$$

Method 1

$$F_{T,1,Rd1} = \frac{4 \cdot M_{pl,1,Rd}}{m_{fc}} = \frac{4 \cdot 3.55kNm}{44.50mm} = 318.77kN$$

Method 2 (alternative method)

Parameter for bearing zone

$$e_w = 0.25 \cdot d_w = 0.25 \cdot 44.00mm = 11.00mm$$

$$F_{T,1,Rd2} = \frac{(8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}}{2 \cdot m_{fc} \cdot n - e_w \cdot (m_{fc} + n)} = \frac{(8 \cdot 51.00mm - 2 \cdot 11.00mm) \cdot 3.55kNm}{2 \cdot 44.50mm \cdot 51.00mm - 11.00mm \cdot (44.50mm + 51.00mm)} = 392.39kN$$

$$F_{T,1,Rd} = \min(F_{T,1,Rd1}; F_{T,1,Rd2}) = \min(318.77kN; 392.39kN) = 318.77kN$$

Model 2: Bolt failure with yielding of the column flange

$$M_{pl,2,Rd} = \frac{0.25 \cdot l_{eff,2} \cdot t_{fc}^2 \cdot f_{yc}}{\gamma_{M0}} = \frac{0.25 \cdot 177.59mm \cdot (15.00mm)^2 \cdot 355.00MPa}{1.00} = 3.55kNm$$

$$F_{T,2,Rd} = \frac{2 \cdot M_{pl,2,Rd} + n \cdot \sum F_{t,Rd}}{m_{fc} + n} = \frac{2 \cdot 3.55kNm + 51.00mm \cdot 2 \cdot 203.33kN}{44.50mm + 51.00mm} = 291.43kN$$

Model 3: Bolt failure

$$F_{T,3,Rd} = \sum F_{t,Rd} = 2 \cdot 203.33kN = 406.66kN$$

Component resistance

$$F_{t,fc,Rd(1)} = \min(F_{T,1,Rd}; F_{T,2,Rd}; F_{T,3,Rd}) = \min(318.77kN; 291.43kN; 406.66kN) = 291.43kN$$

Column web in transverse tension

The section area of column web panel

$$A_{vc} = A_c - 2 \cdot b_{fc} \cdot t_{fc} + (t_{wc} + r_c) \cdot t_{fc} = 78.08cm^2 - 2 \cdot 200.00mm \cdot 15.00mm + (9.00mm + 0.00mm) \cdot 15.00mm = 19.43cm^2$$

The effective width of the column web in tension

$$b_{eff,t,wc} = l_{eff,1(4)} = 177.59mm$$

Reduction factor

$$\omega_1 = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{b_{eff,t,wc} \cdot t_{wc}}{A_{vc}}\right)^2}} = \frac{1}{\sqrt{1 + 1.3 \cdot \left(\frac{177.59 \cdot 9.00mm}{19.43cm^2}\right)^2}} = 0.73$$

$$\omega = \omega_1 = 0.73$$

$$F_{t,wc,Rd,st} = \frac{(b_{fc} - t_{wc}) \cdot t_s \cdot f_{y,s}}{\gamma_{M0}} = \frac{(200.00mm - 9.00mm) \cdot 10.00mm \cdot 355.00MPa}{1.00} = 678.05kN$$

Design resistance of column web subject to transverse tension

$$F_{t,wc,Rd(4)} = \frac{\omega \cdot b_{eff,t,wc} \cdot t_{wc} \cdot f_{y,wc}}{\gamma_{M0}} + F_{t,wc,Rd,st} = \frac{0.73 \cdot 177.59mm \cdot 9.00mm \cdot 355.00MPa}{1.00} + 678.05kN = 1091.91kN$$

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End plate in bending

Geometrical parameters

Bolt distance from outer edge

$$e_{ep} = 36.00mm$$

Bolt distance from beam web

$$m_{ep} = 0.5 \cdot (w - t_{wb}) - 0.8 \cdot \sqrt{2} \cdot a_w = 0.5 \cdot (98.00mm - 8.00mm) - 0.8 \cdot \sqrt{2} \cdot 4.00mm = 40.47mm$$

Distance e_{\min}

$$e_{\min} = \min(e_x; e_{ep}) = \min(36.00mm; 36.00mm) = 36.00mm$$

Calculation parameter n

$$n = \min(e_{\min}; 1.25 \cdot m_{ep}) = \min(36.00mm; 1.25 \cdot 40.47mm) = 35.10mm$$

Bolt distance from beam flange

$$m_x = e_{p1} - e_1 - 0.8 \cdot a_f \cdot \sqrt{2} = 72.00mm - 36.00mm - 0.8 \cdot 7.00mm \cdot \sqrt{2} = 28.08mm$$

Bolt distance from outer horizontal edge plate

$$e_x = e_1 = 36.00mm$$

Effective length for one bolt in circular patterns

$$l_{eff,cp,1} = 2 \cdot \pi \cdot m_x = 2 \cdot \pi \cdot 28.08mm = 176.43mm$$

$$l_{eff,cp,2} = \pi \cdot m_x + w = \pi \cdot 28.08mm + 98.00mm = 186.22mm$$

$$l_{eff,cp,3} = \pi \cdot m_x + 2 \cdot e = \pi \cdot 28.08mm + 2 \cdot 36.00mm = 160.22mm$$

$$l_{eff,cp} = \min(l_{eff,cp,1}; l_{eff,cp,2}; l_{eff,cp,3}) = \min(176.43mm; 186.22mm; 160.22mm) = 160.22mm$$

Effective length for one bolt in non-circular patterns

$$l_{eff,nc,1} = 4 \cdot m_x + 1.25 \cdot e_x = 4 \cdot 28.08mm + 1.25 \cdot 36.00mm = 157.32mm$$

$$l_{eff,nc,2} = e + 2 \cdot m_x + 0.625 \cdot e_x = 36.00mm + 2 \cdot 28.08mm + 0.625 \cdot 36.00mm = 114.66mm$$

$$l_{eff,nc,3} = 0.5 \cdot b_p = 0.5 \cdot 170.00mm = 85.00mm$$

$$l_{eff,nc,4} = 0.5 \cdot w + 2 \cdot m_x + 0.625 \cdot e_x = 0.5 \cdot 98.00mm + 2 \cdot 28.08mm + 0.625 \cdot 36.00mm = 127.66mm$$

$$l_{eff,nc} = \min(l_{eff,nc,1}; l_{eff,nc,2}; l_{eff,nc,3}; l_{eff,nc,4}) = \min(157.32mm; 114.66mm; 85.00mm; 127.66mm) = 85.00mm$$

Effective length for one bolt for 1 mode

$$l_{eff,1} = \min(l_{eff,cp}; l_{eff,nc}) = \min(160.22mm; 85.00mm) = 85.00mm$$

Effective length for one bolt for 2 mode

$$l_{eff,2} = l_{eff,nc} = 85.00mm$$

Model 1: Complete yielding of the end plate

$$M_{pl,1,Rd} = \frac{0.25 \cdot l_{eff,1} \cdot t_p^2 \cdot f_{yp}}{\gamma_{M0}} = \frac{0.25 \cdot 85.00mm \cdot (20.00mm)^2 \cdot 355.00MPa}{1.00} = 3.02kNm$$

Method 1

$$F_{T,1,Rd1} = \frac{4 \cdot M_{pl,1,Rd}}{m_x} = \frac{4 \cdot 3.02kNm}{28.08mm} = 429.84kN$$

Method 2 (alternative method)

Parameter for bearing zone

$$e_w = 0.25 \cdot d_w = 0.25 \cdot 44.00mm = 11.00mm$$

$$F_{T,1,Rd2} = \frac{(8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}}{2 \cdot m_x \cdot n - e_w \cdot (m_x + n)} = \frac{(8 \cdot 35.10mm - 2 \cdot 11.00mm) \cdot 3.02kNm}{2 \cdot 28.08mm \cdot 35.10mm - 11.00mm \cdot (28.08mm + 35.10mm)} = 611.89kN$$

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$$F_{T,1,Rd} = \min(F_{T,1,Rd1}; F_{T,1,Rd2}) = \min(429.84kN; 611.89kN) = 429.84 \text{ kN}$$

Model 2: Bolt failure with yielding of the end plate

$$M_{pl,2,Rd} = \frac{0.25 \cdot l_{eff,2} \cdot t_p^2 \cdot f_{yp}}{\gamma_{M0}} = \frac{0.25 \cdot 85.00mm \cdot (20.00mm)^2 \cdot 355.00MPa}{1.00} = 3.02kNm$$

$$F_{T,2,Rd} = \frac{2 \cdot M_{pl,2,Rd} + n \cdot \sum F_{t,Rd}}{m_x + n} = \frac{2 \cdot 3.02kNm + 35.10mm \cdot 2 \cdot 203.33kN}{28.08mm + 35.10mm} = 321.44kN$$

Model 3: Bolt failure

$$F_{T,3,Rd} = \sum F_{t,Rd} = 2 \cdot 203.33kN = 406.66kN$$

Component resistance

$$F_{t,ep,Rd(1)} = \min(F_{T,1,Rd}; F_{T,2,Rd}; F_{T,3,Rd}) = \min(429.84kN; 321.44kN; 406.66kN) = 321.44 \text{ kN}$$

Resistance of the bolt row 4

Bending resistance

Real bending moment

$$M_0 = M_{b1,Ed} = 113.42kNm$$

The design moment resistance of the joint, assuming no axial force

$$M_{j,Rd} = F_{t,Rd(1)M} \cdot h_1 + F_{t,Rd(2)M} \cdot h_2 + F_{t,Rd(3)M} \cdot h_3 = 282.18kN \cdot 389.65mm + 101.19kN \cdot 304.95mm + 0.00kN \cdot 42.35mm = 140.81kNm$$

$\frac{ M_0 }{M_{j,Rd}} \leq 1$	$0.81 < 1.00$	0.81	
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Shear resistance

Shear force

$$V_0 = -N_{b1,Ed} \cdot \sin(\alpha) + V_{b1,Ed} \cdot \cos(\alpha) = -((-44.28kN)) \cdot \sin(0.00Deg) + 62.88kN \cdot \cos(0.00Deg) = 62.88kN$$

BOLTS ROW 1**Bolt bearing on the column flange**

Coefficient determined by bolt spacing

$$\alpha_{ep} = \min(1.0; \frac{f_{ub}}{f_{uc}}; \frac{e_1}{d_0}) = \min(1.0; \frac{800.00MPa}{510.00MPa}; \frac{36.00mm}{27.00mm}) = 0.44$$

Coefficient determined by bolt spacing

$$k_1 = \min(2.5; 2.8 \cdot \frac{e_2}{d_0}) = \min(2.5; 2.8 \cdot \frac{51.00mm}{27.00mm}) = 2.50$$

Bearing resistance of a bolt

$$F_{b,Rdfc} = \frac{k_1 \cdot \alpha_b \cdot f_{uc} \cdot d \cdot t_{fc}}{\gamma_{M2}} = \frac{2.50 \cdot 0.44 \cdot 510.00MPa \cdot 24.00mm \cdot 15.00mm}{1.25} = 163.20kN$$

Bolt bearing on the plate

Coefficient determined by bolt spacing

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$$\alpha_{ep} = \min\left(1.0; \frac{f_{ub}}{f_{up}}; \frac{e_1}{d_0}\right) = \min\left(1.0; \frac{800.00MPa}{510.00MPa}; \frac{36.00mm}{27.00mm}\right) = 0.44$$

Coefficient determined by bolt spacing

$$k_1 = \min\left(2.5; 2.8 \cdot \frac{e_2}{d_0}\right) = \min\left(2.5; 2.8 \cdot \frac{36.00mm}{27.00mm}\right) = 2.03$$

Bearing resistance of a bolt

$$F_{b,Rdep} = \frac{k_1 \cdot \alpha_b \cdot f_{up} \cdot d \cdot t_p}{\gamma_{M2}} = \frac{2.03 \cdot 0.44 \cdot 510.00MPa \cdot 24.00mm \cdot 20.00mm}{1.25} = 176.98kN$$

Resistance of the bolt row 1

$$V_{Rd(1)} = m_1 \cdot \min(F_{b,Rdfc}; F_{b,Rdep}; F_{v,Rd}) = 2 * \min(163.20kN; 176.98kN; 173.72kN) = 326.40 kN$$

BOLTS ROW 2**Bolt bearing on the column flange**

Coefficient determined by bolt spacing

$$\alpha_{ep} = \min\left(1.0; \frac{f_{ub}}{f_{uc}}; \frac{P_1}{3 \cdot d_0} - 0.25\right) = \min\left(1.0; \frac{800.00MPa}{510.00MPa}; \frac{84.70mm}{3 \cdot 27.00mm} - 0.25\right) = 0.80$$

Coefficient determined by bolt spacing

$$k_1 = \min\left(2.5; 1.4 \cdot \frac{P_2}{d_0} - 1.7\right) = \min\left(2.5; 1.4 \cdot \frac{98.00mm}{27.00mm} - 1.7\right) = 2.50$$

Bearing resistance of a bolt

$$F_{b,Rdfc} = \frac{k_1 \cdot \alpha_b \cdot f_{uc} \cdot d \cdot t_{fc}}{\gamma_{M2}} = \frac{2.50 \cdot 0.80 \cdot 510.00MPa \cdot 24.00mm \cdot 15.00mm}{1.25} = 292.17kN$$

Bolt bearing on the plate

Coefficient determined by bolt spacing

$$\alpha_{ep} = \min\left(1.0; \frac{f_{ub}}{f_{up}}; \frac{P_1}{3 \cdot d_0} - 0.25\right) = \min\left(1.0; \frac{800.00MPa}{510.00MPa}; \frac{84.70mm}{3 \cdot 27.00mm} - 0.25\right) = 0.80$$

Coefficient determined by bolt spacing

$$k_1 = \min\left(2.5; 1.4 \cdot \frac{P_2}{d_0} - 1.7\right) = \min\left(2.5; 1.4 \cdot \frac{98.00mm}{27.00mm} - 1.7\right) = 2.03$$

Bearing resistance of a bolt

$$F_{b,Rdep} = \frac{k_1 \cdot \alpha_b \cdot f_{up} \cdot d \cdot t_p}{\gamma_{M2}} = \frac{2.03 \cdot 0.80 \cdot 510.00MPa \cdot 24.00mm \cdot 20.00mm}{1.25} = 316.85kN$$

Resistance of the bolt row 2

$$V_{Rd(2)} = m_2 \cdot \min(F_{b,Rdfc}; F_{b,Rdep}; F_{v,Rd}) = 2 * \min(292.17kN; 316.85kN; 173.72kN) = 347.44 kN$$

BOLTS ROW 3**Bolt bearing on the column flange**

Coefficient determined by bolt spacing

$$\alpha_{ep} = \min\left(1.0; \frac{f_{ub}}{f_{uc}}; \frac{P_1}{3 \cdot d_0} - 0.25\right) = \min\left(1.0; \frac{800.00MPa}{510.00MPa}; \frac{84.70mm}{3 \cdot 27.00mm} - 0.25\right) = 0.80$$

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Coefficient determined by bolt spacing

$$k_1 = \min(2.5 ; 1.4 \cdot \frac{p_2}{d_0} - 1.7) = \min(2.5 ; 1.4 \cdot \frac{98.00mm}{27.00mm} - 1.7) = 2.50$$

Bearing resistance of a bolt

$$F_{b,Rdfc} = \frac{k_1 \cdot \alpha_b \cdot f_{uc} \cdot d \cdot t_{fc}}{\gamma_{M2}} = \frac{2.50 \cdot 0.80 \cdot 510.00MPa \cdot 24.00mm \cdot 15.00mm}{1.25} = 292.17kN$$

Bolt bearing on the plate

Coefficient determined by bolt spacing

$$\alpha_{ep} = \min(1.0 ; \frac{f_{ub}}{f_{up}} ; \frac{p_1}{3 \cdot d_0} - 0.25) = \min(1.0 ; \frac{800.00MPa}{510.00MPa} ; \frac{84.70mm}{3 \cdot 27.00mm} - 0.25) = 0.80$$

Coefficient determined by bolt spacing

$$k_1 = \min(2.5 ; 1.4 \cdot \frac{p_2}{d_0} - 1.7) = \min(2.5 ; 1.4 \cdot \frac{98.00mm}{27.00mm} - 1.7) = 2.03$$

Bearing resistance of a bolt

$$F_{b,Rdep} = \frac{k_1 \cdot \alpha_b \cdot f_{up} \cdot d \cdot t_p}{\gamma_{M2}} = \frac{2.03 \cdot 0.80 \cdot 510.00MPa \cdot 24.00mm \cdot 20.00mm}{1.25} = 316.85kN$$

Resistance of the bolt row 3

$$V_{Rd(3)} = m_3 \cdot \min(F_{b,Rdfc} ; F_{b,Rdep} ; F_{v,Rd}) = 2 \cdot \min(292.17kN ; 316.85kN ; 173.72kN) = 347.44 kN$$

BOLTS ROW 4**Bolt bearing on the column flange**

Coefficient determined by bolt spacing

$$\alpha_{ep} = \min(1.0 ; \frac{f_{ub}}{f_{uc}} ; \frac{e_1}{d_0}) = \min(1.0 ; \frac{800.00MPa}{510.00MPa} ; \frac{\infty}{27.00mm}) = 1.00$$

Coefficient determined by bolt spacing

$$k_1 = \min(2.5 ; 2.8 \cdot \frac{e_2}{d_0}) = \min(2.5 ; 2.8 \cdot \frac{51.00mm}{27.00mm}) = 2.50$$

Bearing resistance of a bolt

$$F_{b,Rdfc} = \frac{k_1 \cdot \alpha_b \cdot f_{uc} \cdot d \cdot t_{fc}}{\gamma_{M2}} = \frac{2.50 \cdot 1.00 \cdot 510.00MPa \cdot 24.00mm \cdot 15.00mm}{1.25} = 367.20kN$$

Bolt bearing on the plate

Coefficient determined by bolt spacing

$$\alpha_{ep} = \min(1.0 ; \frac{f_{ub}}{f_{up}} ; \frac{e_1}{d_0}) = \min(1.0 ; \frac{800.00MPa}{510.00MPa} ; \frac{36.00mm}{27.00mm}) = 0.44$$

Coefficient determined by bolt spacing

$$k_1 = \min(2.5 ; 2.8 \cdot \frac{e_2}{d_0}) = \min(2.5 ; 2.8 \cdot \frac{36.00mm}{27.00mm}) = 2.03$$

Bearing resistance of a bolt

$$F_{b,Rdep} = \frac{k_1 \cdot \alpha_b \cdot f_{up} \cdot d \cdot t_p}{\gamma_{M2}} = \frac{2.03 \cdot 0.44 \cdot 510.00MPa \cdot 24.00mm \cdot 20.00mm}{1.25} = 176.98kN$$

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Resistance of the bolt row 4

$$V_{Rd(4)} = m_4 \cdot \min(F_{b,Rdfc}; F_{b,Rdep}; F_{v,Rd}) = 2 * \min(367.20kN; 176.98kN; 173.72kN) = 347.44 \text{ kN}$$

$$V_{j,Rd} = V_{Rd(1)} + V_{Rd(2)} + V_{Rd(3)} + V_{Rd(4)} = 326.40kN + 347.44kN + 347.44kN + 347.44kN = 1368.71kN$$

$\frac{ V_0 }{V_{j,Rd}} \leq 1$	$ 62.88kN < 1368.71kN$	0.05	✓
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Fillet welds connecting beam and front plate

Forces in welds

Axial force

$$N_0 = N_{b1,Ed} \cdot \cos(\alpha) + V_{b1,Ed} \cdot \sin(\alpha) = (-44.28kN) \cdot \cos(0.00Deg) + 62.88kN \cdot \sin(0.00Deg) = -44.28kN$$

Shear force

$$V_0 = -N_{b1,Ed} \cdot \sin(\alpha) + V_{b1,Ed} \cdot \cos(\alpha) = -((-44.28kN)) \cdot \sin(0.00Deg) + 62.88kN \cdot \cos(0.00Deg) = 62.88kN$$

Real bending moment

$$M_0 = M_{b1,Ed} = 113.42kNm$$

Geometric properties of welds

Beam

Area of horizontal welds on upper flange

$$A_{wfu} = [2 \cdot (b_{fb} - r_b) - t_{wb}] \cdot a_f = [2 \cdot (170.00mm - 0.00mm) - 8.00mm] \cdot 7.00mm = 23.24cm^2$$

Area of horizontal welds on lower flange

$$A_{wfl} = [2 \cdot (b_{fb} - r_b) - t_{wb}] \cdot a_f = [2 \cdot (170.00mm - 0.00mm) - 8.00mm] \cdot 7.00mm = 23.24cm^2$$

Area of vertical welds

$$A_{ww} = 2 \cdot \frac{h_b - 2 \cdot (t_{fb} + r_b)}{\cos(\alpha)} \cdot a_w = 2 \cdot \frac{360.00mm - 2 \cdot (12.70mm + 0.00mm)}{\cos(0.00Deg)} \cdot 4.00mm = 26.77cm^2$$

Area of all welds

$$A_w = A_{wfu} + A_{wfl} + A_{ww} = 23.24cm^2 + 23.24cm^2 + 26.77cm^2 = 73.25cm^2$$

Offset of welds centroid with respect to beam centroid

$$e_{0w} = 0.00mm$$

Moment of inertia welds

$$I_w = 16598.43cm^4$$

The point where the stresses are checked

$$z_i = 183.50mm$$

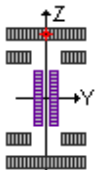
Work: Example Model

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Elastic modulus of welds	
$W_w = 904.55\text{cm}^3$	
Stress from axial force	
$\sigma_N = \frac{N_0}{A_w} = \frac{-44.28\text{kN}}{73.25\text{cm}^2} = -6.05\text{MPa}$	
Stress due to bending	
$\sigma_M = \frac{M_0 \cdot z_i}{I_w} = \frac{113.42\text{kNm} \cdot 183.50\text{mm}}{16598.43\text{cm}^4} = 125.39\text{MPa}$	
Maximum normal stress	
$\sigma = \sigma_N + \sigma_M = -6.05\text{MPa} + 125.39\text{MPa} = 119.34\text{MPa}$	
Normal perpendicular stress	
$\sigma_{\perp} = \frac{\sigma}{\sqrt{2}} = \frac{119.34\text{MPa}}{\sqrt{2}} = 84.39\text{MPa}$	
Perpendicular tangent stress	
$\tau_{\perp} = \frac{\sigma}{\sqrt{2}} = \frac{119.34\text{MPa}}{\sqrt{2}} = 84.39\text{MPa}$	

Welds resistance coefficient

$\beta_w = 0.90$

$ \sigma_{\perp} \leq \frac{0.9 \cdot f_u}{\gamma_{M2}}$	$ 84.39\text{MPa} < 367.20\text{MPa}$	0.17	✓
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$\sqrt{\sigma_{\perp}^2 + 3 \cdot (\tau_{\perp}^2)} \leq \frac{f_u}{\beta_w \cdot \gamma_{M2}}$	$168.77\text{MPa} < 453.33\text{MPa}$	0.37	✓
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The point where the stresses are checked	$z_i = 167.30\text{mm}$
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Work: Example Model

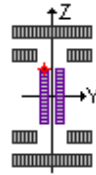
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Elastic modulus of welds	
$W_w = 992.14 \text{ cm}^3$	
Stress from axial force	
$\sigma_N = \frac{N_0}{A_w} = \frac{-44.28 \text{ kN}}{73.25 \text{ cm}^2} = -6.05 \text{ MPa}$	
Stress due to bending	
$\sigma_M = \frac{M_0 \cdot z_i}{I_w} = \frac{113.42 \text{ kNm} \cdot 167.30 \text{ mm}}{16598.43 \text{ cm}^4} = 114.32 \text{ MPa}$	
Maximum normal stress	
$\sigma = \sigma_N + \sigma_M = -6.05 \text{ MPa} + 114.32 \text{ MPa} = 108.27 \text{ MPa}$	
Normal perpendicular stress	
$\sigma_{\perp} = \frac{\sigma}{\sqrt{2}} = \frac{108.27 \text{ MPa}}{\sqrt{2}} = 76.56 \text{ MPa}$	
Perpendicular tangent stress	
$\tau_{\perp} = \frac{\sigma}{\sqrt{2}} = \frac{108.27 \text{ MPa}}{\sqrt{2}} = 76.56 \text{ MPa}$	
Parallel tangent stress	
$\tau_{\parallel} = \frac{V_0}{A_{ww}} = \frac{62.88 \text{ kN}}{26.77 \text{ cm}^2} = 23.49 \text{ MPa}$	



Welds resistance coefficient

$\beta_w = 0.90$

$ \sigma_{\perp} \leq \frac{0.9 \cdot f_u}{\gamma_{M2}}$	$ 76.56 \text{ MPa} < 367.20 \text{ MPa}$	0.15	✓
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$\sqrt{\sigma_{\perp}^2 + 3 \cdot (\tau_{\perp}^2 + \tau_{\parallel}^2)} \leq \frac{f_u}{\beta_w \cdot \gamma_{M2}}$	$158.43 \text{ MPa} < 453.33 \text{ MPa}$	0.35	✓
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The point where the stresses are checked	$z_i = -167.30 \text{ mm}$
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Work: Example Model

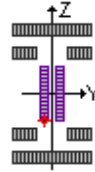
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Elastic modulus of welds	
$W_w = 992.14 \text{cm}^3$	
Stress from axial force	
$\sigma_N = \frac{N_0}{A_w} = \frac{-44.28 \text{kN}}{73.25 \text{cm}^2} = -6.05 \text{MPa}$	
Stress due to bending	
$\sigma_M = \frac{M_0 \cdot z_i}{I_w} = \frac{113.42 \text{kNm} \cdot (-167.30 \text{mm})}{16598.43 \text{cm}^4} = -114.32 \text{MPa}$	
Maximum normal stress	
$\sigma = \sigma_N + \sigma_M = -6.05 \text{MPa} + (-114.32 \text{MPa}) = -120.36 \text{MPa}$	
Normal perpendicular stress	
$\sigma_{\perp} = \frac{\sigma}{\sqrt{2}} = \frac{-120.36 \text{MPa}}{\sqrt{2}} = -85.11 \text{MPa}$	
Perpendicular tangent stress	
$\tau_{\perp} = \frac{\sigma}{\sqrt{2}} = \frac{-120.36 \text{MPa}}{\sqrt{2}} = -85.11 \text{MPa}$	
Parallel tangent stress	
$\tau_{\parallel} = \frac{V_0}{A_{ww}} = \frac{62.88 \text{kN}}{26.77 \text{cm}^2} = 23.49 \text{MPa}$	



Welds resistance coefficient

$\beta_w = 0.90$

$ \sigma_{\perp} \leq \frac{0.9 \cdot f_u}{\gamma_{M2}}$	$ -85.11 \text{MPa} < 367.20 \text{MPa}$	0.17	✓
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$\sqrt{\sigma_{\perp}^2 + 3 \cdot (\tau_{\perp}^2 + \tau_{\parallel}^2)} \leq \frac{f_u}{\beta_w \cdot \gamma_{M2}}$	$175.01 \text{MPa} < 453.33 \text{MPa}$	0.39	✓
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The point where the stresses are checked	$z_i = -183.50 \text{mm}$
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Elastic modulus of welds	
$W_w = 904.55\text{cm}^3$	
Stress from axial force	
$\sigma_N = \frac{N_0}{A_w} = \frac{-44.28\text{kN}}{73.25\text{cm}^2} = -6.05\text{MPa}$	
Stress due to bending	
$\sigma_M = \frac{M_0 \cdot z_i}{I_w} = \frac{113.42\text{kNm} \cdot (-183.50\text{mm})}{16598.43\text{cm}^4} = -125.39\text{MPa}$	
Maximum normal stress	
$\sigma = \sigma_N + \sigma_M = -6.05\text{MPa} + (-125.39\text{MPa}) = -131.43\text{MPa}$	
Normal perpendicular stress	
$\sigma_{\perp} = \frac{\sigma}{\sqrt{2}} = \frac{-131.43\text{MPa}}{\sqrt{2}} = -92.94\text{MPa}$	
Perpendicular tangent stress	
$\tau_{\perp} = \frac{\sigma}{\sqrt{2}} = \frac{-131.43\text{MPa}}{\sqrt{2}} = -92.94\text{MPa}$	

Welds resistance coefficient

$$\beta_w = 0.90$$

$ \sigma_{\perp} \leq \frac{0.9 \cdot f_u}{\gamma_{M2}}$	$ -92.94\text{MPa} < 367.20\text{MPa}$	0.18	✓
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$\sqrt{\sigma_{\perp}^2 + 3 \cdot (\tau_{\perp}^2)} \leq \frac{f_u}{\beta_w \cdot \gamma_{M2}}$	$185.87\text{MPa} < 453.33\text{MPa}$	0.41	✓
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The rotational stiffness of a joint

Column web panel in shear

$$k_1 = \frac{0.385 \cdot A_{vc}}{\beta \cdot h} = \frac{0.385 \cdot 19.43\text{cm}^2}{1.00 \cdot 360.00\text{mm}} = 2.13\text{mm}$$

Column web in transverse compression

$$k_2 = \infty \text{ mm}$$

The bolt elongation length

$$L_b = t_p + t_{fc} + 0.5 \cdot (m + k) + 2 \cdot t_{wa} = 20.00\text{mm} + 15.00\text{mm} + 0.5 \cdot (22.30\text{mm} + 15.00\text{mm}) + 2 \cdot 4.00\text{mm} = 61.65\text{mm}$$

Bolt tension

$$k_{10} = \frac{3.2 \cdot A_s}{L_b} = \frac{3.2 \cdot 3.53\text{cm}^2}{61.65\text{mm}} = 9.16\text{mm}$$

The depth of the column web

$$d_c = h_c - 2 \cdot (t_{fc} + r_c) = 200.00\text{mm} - 2 \cdot (15.00\text{mm} + 0.00\text{mm}) = 170.00\text{mm}$$

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Row 1

Column web in transverse tension

$$k_{3(1)} = \frac{0.7 \cdot b_{\text{eff},wc,t} \cdot t_{wc}}{d_c} = \frac{0.7 \cdot 157.21\text{mm} \cdot 9.00\text{mm}}{170.00\text{mm}} = 5.83\text{mm}$$

Column flange in bending

$$k_{4(1)} = \frac{0.9 \cdot l_{\text{eff},fc,t} \cdot t_{fc}^3}{m^3} = \frac{0.9 \cdot 157.21\text{mm} \cdot (15.00\text{mm})^3}{(44.50\text{mm})^3} = 5.42\text{mm}$$

End plate in bending

$$k_{5(1)} = \frac{0.9 \cdot l_{\text{eff},p} \cdot t_p^3}{m_x^3} = \frac{0.9 \cdot 85.00\text{mm} \cdot (20.00\text{mm})^3}{(28.08\text{mm})^3} = 27.64\text{mm}$$

$$k_{\text{eff}(1)} = \frac{1}{\frac{1}{k_{3(1)}} + \frac{1}{k_{4(1)}} + \frac{1}{k_{5(1)}} + \frac{1}{k_{10}}} = \frac{1}{\frac{1}{5.83\text{mm}} + \frac{1}{5.42\text{mm}} + \frac{1}{27.64\text{mm}} + \frac{1}{9.16\text{mm}}} = 1.99\text{mm}$$

Row 2

Column web in transverse tension

$$k_{3(2)} = \frac{0.7 \cdot b_{\text{eff},wc,t} \cdot t_{wc}}{d_c} = \frac{0.7 \cdot 241.75\text{mm} \cdot 9.00\text{mm}}{170.00\text{mm}} = 8.96\text{mm}$$

Column flange in bending

$$k_{4(2)} = \frac{0.9 \cdot l_{\text{eff},fc,t} \cdot t_{fc}^3}{m^3} = \frac{0.9 \cdot 241.75\text{mm} \cdot (15.00\text{mm})^3}{(44.50\text{mm})^3} = 8.33\text{mm}$$

End plate in bending

$$k_{5(2)} = \frac{0.9 \cdot l_{\text{eff},p} \cdot t_p^3}{m^3} = \frac{0.9 \cdot 238.05\text{mm} \cdot (20.00\text{mm})^3}{(40.47\text{mm})^3} = 25.85\text{mm}$$

$$k_{\text{eff}(2)} = \frac{1}{\frac{1}{k_{3(2)}} + \frac{1}{k_{4(2)}} + \frac{1}{k_{5(2)}} + \frac{1}{k_{10}}} = \frac{1}{\frac{1}{8.96\text{mm}} + \frac{1}{8.33\text{mm}} + \frac{1}{25.85\text{mm}} + \frac{1}{9.16\text{mm}}} = 2.64\text{mm}$$

Row 3

Column web in transverse tension

$$k_{3(3)} = \frac{0.7 \cdot b_{\text{eff},wc,t} \cdot t_{wc}}{d_c} = \frac{0.7 \cdot 241.75\text{mm} \cdot 9.00\text{mm}}{170.00\text{mm}} = 8.96\text{mm}$$

Column flange in bending

$$k_{4(3)} = \frac{0.9 \cdot l_{\text{eff},fc,t} \cdot t_{fc}^3}{m^3} = \frac{0.9 \cdot 241.75\text{mm} \cdot (15.00\text{mm})^3}{(44.50\text{mm})^3} = 8.33\text{mm}$$

End plate in bending

$$k_{5(3)} = \frac{0.9 \cdot l_{\text{eff},p} \cdot t_p^3}{m^3} = \frac{0.9 \cdot 206.90\text{mm} \cdot (20.00\text{mm})^3}{(40.47\text{mm})^3} = 22.47\text{mm}$$

$$k_{\text{eff}(3)} = \frac{1}{\frac{1}{k_{3(3)}} + \frac{1}{k_{4(3)}} + \frac{1}{k_{5(3)}} + \frac{1}{k_{10}}} = \frac{1}{\frac{1}{8.96\text{mm}} + \frac{1}{8.33\text{mm}} + \frac{1}{22.47\text{mm}} + \frac{1}{9.16\text{mm}}} = 2.60\text{mm}$$

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Lever arm of internal forces

$$z_{eq} = \frac{k_{eff(1)} \cdot h_1^2 + k_{eff(2)} \cdot h_2^2 + k_{eff(3)} \cdot h_3^2}{k_{eff(1)} \cdot h_1 + k_{eff(2)} \cdot h_2 + k_{eff(3)} \cdot h_3} = \frac{1.99mm \cdot (389.65mm)^2 + 2.64mm \cdot (304.95mm)^2 + 2.60mm \cdot (42.35mm)^2}{1.99mm \cdot 389.65mm + 2.64mm \cdot 304.95mm + 2.60mm \cdot 42.35mm} = 326.80mm$$

Equivalent stiffness coefficient

$$k_{eq} = \frac{k_{eff(1)} \cdot h_1 + k_{eff(2)} \cdot h_2 + k_{eff(3)} \cdot h_3}{z_{eq}} = \frac{1.99mm \cdot 389.65mm + 2.64mm \cdot 304.95mm + 2.60mm \cdot 42.35mm}{326.80mm} = 5.17mm$$

The initial rotational stiffness of a joint

$$S_{j,ini} = \frac{E \cdot z_{eq}^2}{\frac{1}{k_1} + \frac{1}{k_2} + \frac{1}{k_{eq}}} = \frac{210000.00MPa \cdot (326.80mm)^2}{\frac{1}{2.13mm} + \frac{1}{\infty mm} + \frac{1}{5.17mm}} = 33792.50 \frac{kNm}{rad}$$

The rotational stiffness of a pinned joint

$$S_{j,pin} = \frac{0.5 \cdot E \cdot I_{yb}}{L_b} = \frac{0.5 \cdot 210000.00MPa \cdot 16270.00cm^4}{3048.01mm} = 5604.81 \frac{kNm}{rad}$$

The rotational stiffness of a rigid joint

$$S_{j,rig} = \frac{k_b \cdot E \cdot I_{yb}}{L_b} = \frac{8.00 \cdot 210000.00MPa \cdot 16270.00cm^4}{3048.01mm} = 89676.99 \frac{kNm}{rad}$$

Stiffness ratio

$$\mu = \left(\frac{1.5 \cdot |M_{b1,Ed}|}{M_{Rd}} \right)^\psi = \left(\frac{1.5 \cdot |113.42kNm|}{140.81kNm} \right)^{2.7} = 1.67$$

The rotational stiffness of a joint

$$S_j = \frac{S_{j,ini}}{\mu} = \frac{33792.50 \frac{kNm}{rad}}{1.67} = 20278.29 \frac{kNm}{rad}$$

Classification of joint

Semi – rigid